

2011-12 PreAP Harmonic Motion 4

1. Remembering that $1000\text{ g} = 1\text{ kg}$, what is the period of a spring that has a 400 g mass and a spring constant of 120 N/m ?

2. * A spring-mass system has a period of 2.5 seconds and a spring constant that is 65 N/m . How much mass is attached?

From the lab:

3. Give two ways to change the period of a spring-mass system.

Example: How long is a pendulum that has a period of 3.2 seconds?

$$T = 2\pi\sqrt{\frac{\ell}{g}}$$

$$3.2 = 6.28\sqrt{\frac{\ell}{10}}$$

$$\frac{3.2}{6.28} = \frac{\cancel{6.28}}{\cancel{6.28}}\sqrt{\frac{\ell}{10}}$$

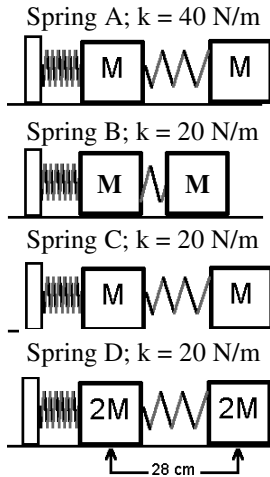
$$0.5096 = \sqrt{\frac{\ell}{10}}$$

$$(0.5096)^2 = \frac{\ell}{10}$$

$$0.2597 = \frac{\ell}{10}$$

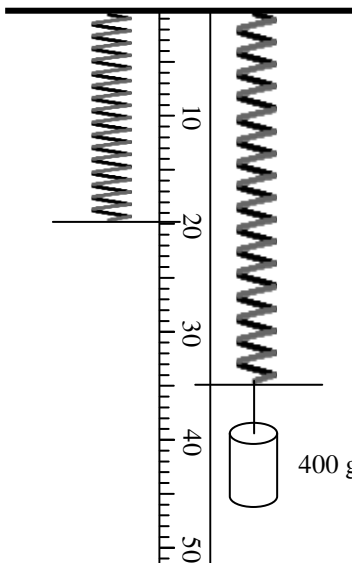
$$10(0.2597) = \ell$$

$$\ell = 2.597\text{ m} = 259.7\text{ cm}$$



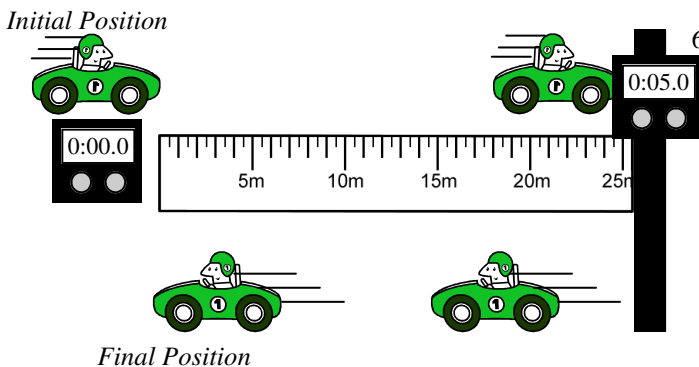
4. The spring-mass systems at the left are shown at their left and right-most positions.

- Which spring has a faster period: A or B?
- Which spring has a faster period: B or C?
- Which spring has a faster period: C or D?
- Which spring has a faster period: A or D?
- What is the amplitude of spring D?
- If spring C has a period of 0.33 seconds, calculate its frequency.
- If $m = 1.5\text{ kg}$, calculate the period of spring D.
- How far does Spring D travel in one full period?
- What is the displacement of Spring D after two full cycles?



5. A spring is unstretched to begin with, but the coils of the spring are not touching. Then a 400 g mass is attached and stretches the spring as shown. Remember that the spring constant has the units of N/m .

- Its original (relaxed) position is known as its equilibrium position. What is the spring's equilibrium position (in m)?
- * x is the displacement from this equilibrium position. In this case, what is x ?
- * Calculate the force pulling down on the spring.
- * Given that $F = -kx$ and that k is always a positive number (a constant), calculate the spring stiffness constant for the spring.
- Now that you have both m and k , calculate the period of the spring.



- A bumper car goes a certain distance, bumps off the wall and comes back to its initial position.
 - * How far did it go in total (total **distance** there and back)?
 - If it took 5 seconds to go to the wall and it stays at constant speed, how long did it take for the whole journey?
 - Calculate the speed of the object.

2. 10.3kg
5B. 15 cm
5C = mg
5D 26.7 N/m
6A 50 m