

PreAP Two Dimensions 5

When you add vectors: 1) set up the vector with the angle starting at the +x axis; 2) calculate each x-component using $H\cos\theta$; 3) calculate each y-component using $H\sin\theta$; 4) total up the x's and y's, remembering to keep track of +s and -s; 5) using x_{total} and y_{total} calculate the resultant's hypotenuse with Pythagorean Theorem and its angle with inverse tangent. When do we use this process? ALWAYS! ALWAYS! ALWAYS! Do I make myself clear?

1. All of these vectors are given with correct angles already, you do not need to change the angles.

A. Calculate the x and y components of the given vectors. DO NOT DRAW THEM—do this with your calculator only.

Vector 1: 250m at 35°

X component

Y-component

Vector 2: 85m at 256°

B. Add together all of your x-components to find x-total.

Vector 3: 424m at 346°

C. Add together all of your y-components to find y-total.

Vector 4: 34 m at 90°

Totals:

D. Use Pythagorean theorem to find the magnitude (size) of the resultant.

Resultant: Magnitude =

Direction =

E. Use inverse tangent to find the direction of the resultant.

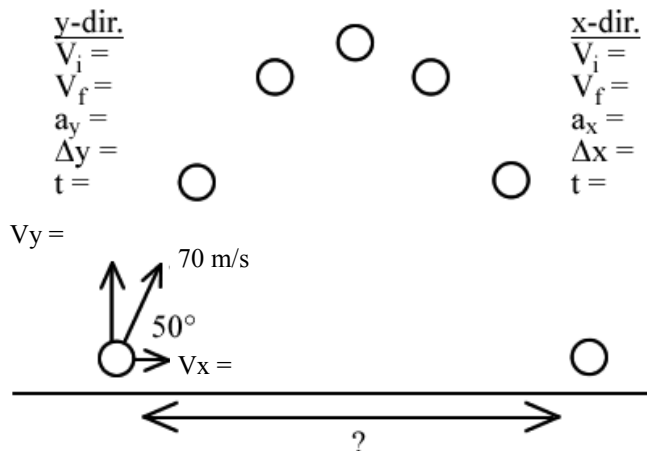
Remember that the negative of a vector means turn the vector around (or put the arrow on the opposite end of the vector). So, the negative direction of 30° is $30^\circ + 180^\circ = 210^\circ$.

2. Given these vectors: A = 425 m at 75° ; B = 68 m at 130° ; C = 91 m at -319° ; D = 213 m at 234° .

Using the same procedure as above, add together these vectors: $A - 3B + 2C + D$.

A. Calculate each of the vectors: A, -3B, etc. and write them below.

B. Then do the table above with each.



3. An object is thrown 70 m/s at 50° , from the ground to the ground.

A. Calculate V_y and V_x .

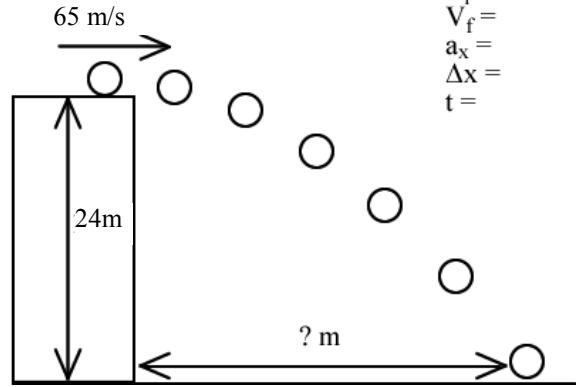
B. Fill in the variables on the chart.

C. Calculate how far away the object lands.

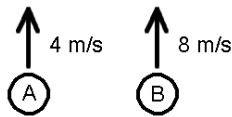
4. An object is shot horizontally from a 24 m cliff going 65 m/s. How far away does it land?

y-dir.
 $V_i =$
 $V_f =$
 $a_y =$
 $\Delta y =$
 $t =$

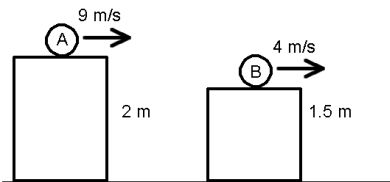
x-dir.
 $V_i =$
 $V_f =$
 $a_x =$
 $\Delta x =$
 $t =$



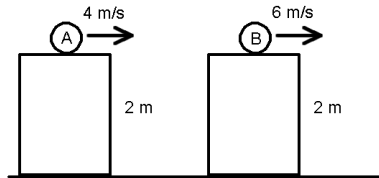
5. A person jumps from the top of a house onto a ground level trampoline. They rebound off of the trampoline going 12 m/s at an angle of 52°. (Draw the diagram and write out the variables.)
- A. Calculate the person's "hang time"
- B. How far away do they land from the trampoline?



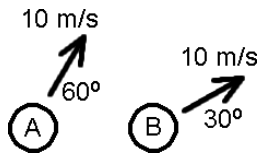
6. Object A or B?
- A. ___ Which has the greatest vertical acceleration?
- B. ___ Which has the greater maximum height?



8. Which has the greatest "hang time": object A or B?



7. Object A or B?
- A. ___ Has the greatest range (greatest Δx)?
- B. ___ Hits the ground first?
- C. ___ Has the greatest initial y-velocity?
- D. ___ Has the greatest magnitude of velocity?



9. Object A or B?
- A. ___ Has the greatest V_y ?
- B. ___ Is in the air for the most time?
- C. ___ Has the greatest V_x ?

10. Here are the things that we know about projectile motion ALWAYS: (some will be with variables only)
- A. a_y always =
- B. a_x always =
- C. If given V and θ , V_{y_i} always =
- D. V_{x_i} always =
- D. If shot from the ground to the ground $\Delta y =$
- E. The x equation always =

Let me show you how you can solve harder problems with this process.

11. A projectile is shot from the ground to the ground. It is in the air for 3.5 seconds and travels 54 meters.
 - A. Assign any variable you know AND write the equation you know you are going to use in the x-direction.
 - B. Using what you learned in Q5, write V_i and V_f in the y-direction using variables.
 - C. Solve for the initial velocity and direction of the object.

