

Supplement: Harmonic Motion Equations

Period vs. Frequency

The **period** is how long it takes to complete one cycle.
 The **frequency** is how many cycles occur per second.
Hertz (Hz) means cycles per second.

$\text{Period (in secs)} \rightarrow T = \frac{1}{f} \quad \text{OR} \quad f = \frac{1}{T} \leftarrow \text{Period (in secs)}$
$\text{Frequency (in hertz)}$

If you know frequency you can find period.

<i>Ex: A wave has a frequency of 10 Hz. Find its period.</i>	
$f = 10 \text{ Hz}$ $T = ?$	$T = 1/f$ $T = 1/10 \text{ Hz}$ $T = 0.1 \text{ sec}$

If you know period you can find frequency.

<i>Ex: A pendulum has a period of 0.5 seconds. Find its frequency.</i>	
$T = 0.5 \text{ sec}$ $f = ?$	$f = 1/T$ $f = 1/0.5 \text{ sec}$ $f = 2 \text{ Hz}$

Harmonics

f_f – is the frequency of the **fundamental** (in Hz).
 f_{Hx} – is the frequency of the **harmonic** (in Hz).
 X – is the number of the harmonic (if H_3 , $X = 3$)

Frequency of Harmonics

$\text{Frequency of harmonic } x \text{ (in Hz)} \rightarrow f_{Hx} = f_f(X) \leftarrow \text{\# of the Harmonic}$
$\text{Frequency of the fundamental (in Hz)}$

If you are given the fundamental you can find the frequencies of any of the harmonics.

<i>Ex. Find the frequency of the fourth harmonic (H_4) of a 6 Hz fundamental.</i>	
$f_f = 6 \text{ Hz}$ $X = 4$ (fourth) $f_{H4} = ?$	$f_{Hx} = f_f(X)$ $f_{H4} = (6 \text{ Hz}) \times (4)$ $f_{H4} = 24 \text{ Hz}$

If you are given the harmonic frequency and what harmonic it is you can find the frequency of the fundamental.

<i>Ex. If the eighth harmonic has a frequency of 80 Hz, find the fundamental frequency.</i>	
$f_{H8} = 80 \text{ Hz}$ $X = 8$ $f_f = ?$	$f_{Hx} = f_f(X)$ $f_f = f_{Hx}/X = 80 \text{ Hz}/8$ $f_f = 10 \text{ Hz}$

Speed of a Wave

λ – is lambda (Greek); used for wavelength: the length of one wave cycle.
 v – is velocity, but here we use it for speed, too.

The Speed (velocity) of a Wave

$\text{velocity (m/sec)} \rightarrow v = f \lambda \leftarrow \begin{matrix} \text{wavelength (m)} \\ \text{frequency (Hz)} \end{matrix}$

You can find speed from frequency and wavelength.

<i>Ex. Find the speed of a 60 Hz wave if one cycle is 4 meters long.</i>	
$f = 60 \text{ Hz}$ $\lambda = 4 \text{ m}$ $v = ?$	$v = f \lambda$ $v = (60 \text{ Hz}) \times (4 \text{ m})$ $v = 240 \text{ m/s}$

You can find either wavelength or frequency if you know the wave's speed.

<i>Ex. What wavelength wave has a 200 m/s velocity and 50 Hz frequency?</i>	
$f = 50 \text{ Hz}$ $v = 200 \text{ m/s}$ $\lambda = ?$	$v = f \lambda$ SO $\lambda = v/f$ $\lambda = (200 \text{ m/s}) \div (50 \text{ Hz})$ $\lambda = 4 \text{ m}$

Speed of Sound (v_s)

The **Speed of Sound in air** is approximately **340 m/sec**.
 Use this number anytime a problem refers to a sound wave, music, a noise, or someone hearing something.

The Speed of a Sound Wave

340 m/sec = $f \lambda$

Speed

$S = \frac{D}{T}$

Because you know the speed of sound, if you know λ you can find f and vice versa.

<i>Ex. Find the wavelength of a 100 Hz sound.</i>	
$v_s = 340 \text{ m/s}$ $f = 100 \text{ Hz}$ $\lambda = ?$	$v = f \lambda$ so $\lambda = v/f$ $\lambda = (340 \text{ m/s}) \div (100 \text{ Hz})$ $\lambda = 3.4 \text{ m}$

If you know how long it takes a sound to reach you, you can find how far away the sound source is.

<i>Ex. If you hear a sound 2 seconds after you see the motion, how far away is it?</i>	
$v_s = 340 \text{ m/s}$ $T = 2 \text{ sec}$ $D = ?$	$v_s = D/T$ SO $D = v_s T$ $D = (340 \text{ m/s}) \times (2 \text{ sec})$ $D = 680 \text{ m}$

Name: _____

Period: _____

Decibels (Loudness)

A + 10 dB change we hear as twice as loud.

A - 10 dB change we hear as half as loud.

Ex. How much louder is a 50 dB noise than a 40 dB noise?

Ex. How much softer is a 25 dB noise than a 35 dB noise?

50 dB - 40 dB = +10 dB
50 dB is twice as loud as 40

25 dB - 35 dB = -10 dB
25 dB is half as loud as 35 dB.

Amplitude

2 ways: 1) **Amplitude** = $\frac{1}{2}(\text{high} - \text{low})$ OR 2) $\frac{1}{2}(\text{peak to peak})$. (Distance from trough to crest divided by 2)

Ex. Crest is at 3 cm; Trough is at -5 cm. Find amplitude.

Way 1) $A = \frac{1}{2}(3\text{cm} - (-5\text{cm})) = \frac{1}{2}(3\text{cm} + 5\text{cm}) = \frac{1}{2}(8) = 4\text{ cm.}$

Way 2) From -5 to 0 = 5cm 5 + 3 = 8.
 $A = \frac{1}{2}(8) = 4\text{ cm}$

What is the period of a 4 Hz wave?

What is the speed of a 10 Hz wave that's wavelength is 25 m?

What is the frequency of a wave with a 2 second period?

How much louder is a 45 dB sound than a 35 dB sound?

If a noise drops from 80 dB to 70 dB, how do we hear the change?

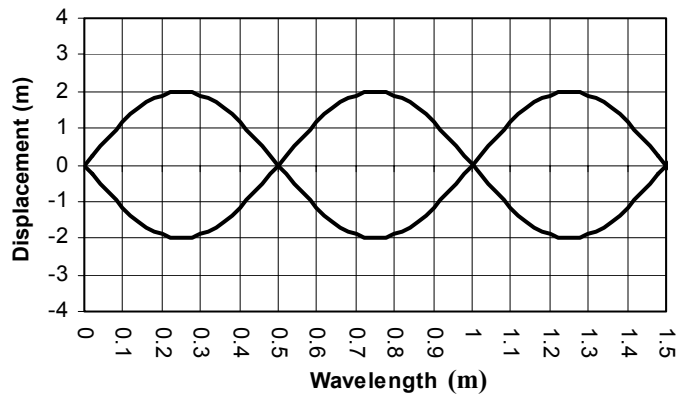
If a standing wave's fundamental is 12 Hz what is the frequency of harmonic 4? (And how many antinodes will harmonic 4 have?)

You hear a hammer 5 seconds after you see it move. How far away is the hammer?

A sound wave has a 10 m wavelength. Find its frequency.

If a noise has a frequency of 17 Hz, find its wavelength.

Standing wave (Harmonic)



Use the above graph to answer the following questions:

What harmonic is it? _____

Mark the nodes and antinodes: _____

If its frequency is 60 Hz find its period: _____

Could a human hear this frequency? _____

Find the fundamental frequency:

Find the 4th harmonic frequency:

What is the amplitude of the wave? _____

What is the wavelength of the wave? _____

The total length of the standing wave is how many wavelengths?
